

7.4 #25-28, 33,34,59

7.5 #1-3, 9-11, 43,45,47

only solve for $0 \leq \theta < 2\pi$

1. Using a **Pythagorean identity** we see that the equation

$\sin x + \sin^2 x + \cos^2 x = 1$ is equivalent to the basic equation

$$\sin x + 1 = 1$$

$$\sin x = 0$$

whose solutions are $x =$

$$0, \pi$$

Use Pythagorean and Double Angle identities to rewrite the given equations in 7.5, then factor and solve.

only solve for $0 \leq \theta < 2\pi$

2. Using a Double Angle identity we see that the equation $\sin x + \sin 2x = 0$ is equivalent to the equation $\sin x + \underbrace{2 \sin x \cos x}_{\text{double angle}}$

Factoring, we see that solving this equation is equivalent to solving two basic equations $\sin x = 0$ and $1 + 2 \cos x = 0$

$$\sin x (1 + 2 \cos x) = 0$$

Use Pythagorean and Double Angle identities to rewrite the given equations in 7.5, then factor and solve.

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3. $2(\cos^2 \theta) + \sin \theta = 1$

$2(1 - \sin^2 \theta) + \sin \theta = 1$

$\underline{2} - 2\sin^2 \theta + \sin \theta - \underline{1} = 0$

$-2\sin^2 \theta + \sin \theta + 1 = 0$ multiply by -1

$2\sin^2 \theta - \sin \theta - 1 = 0$ now factor

$(\quad) (\quad) = 0$ (FOIL)

*Pythagorean Identities:

$\sin^2 \theta + \cos^2 \theta = 1$

$\hookrightarrow \cos^2 \theta = 1 - \sin^2 \theta$

CHECK EVEN AND ODD ANSWERS

7.4 #25-28, 33,34,59

7.5 #1-3, 9-11, 43,45,47

ONLY solve for specific solutions
in the interval: $0 \leq \theta < 2\pi$

(NO general solutions: you don't
have to use $2\pi k$)

CHECK 7.4 #25-28, 33, 34:

(odds and evens are included)

$$\frac{3\pi}{2} \quad \frac{\pi}{3} \quad \frac{2\pi}{3} \quad \frac{4\pi}{3} \quad \frac{5\pi}{3}$$

$$\frac{\pi}{4} \quad \frac{\pi}{4} \quad \frac{3\pi}{4} \quad \frac{5\pi}{4} \quad \frac{5\pi}{4}$$

$$\frac{7\pi}{4} \quad \frac{7\pi}{4} \quad \frac{7\pi}{4} \quad \pi$$

#59 → use degrees
(check answers in book)

CHECK 7.5 #1-3, 9-11:

(odds and evens are included)

$$0 \quad \pi \quad \pi \quad \frac{\pi}{2} \quad \frac{\pi}{3} \quad \frac{5\pi}{3}$$

$$\frac{\pi}{4} \quad \frac{3\pi}{4} \quad \frac{5\pi}{4} \quad \frac{7\pi}{4}$$

$$\frac{\pi}{6} \quad \frac{5\pi}{6} \quad \frac{7\pi}{6} \quad \frac{11\pi}{6}$$

#43,45,47 → check answers in book